Circle Loss: A Unified Perspective of Pair Similarity Optimization

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Introduction

Feature learning:

- maximize the within-class similarity s_p
- minimize the between-class similarity s_n

Many popular losses, e.g., triplet loss:

embed s_n and s_p into similarity pairs and seek to make $(s_n - s_p) < m$ (symmetric optimization)

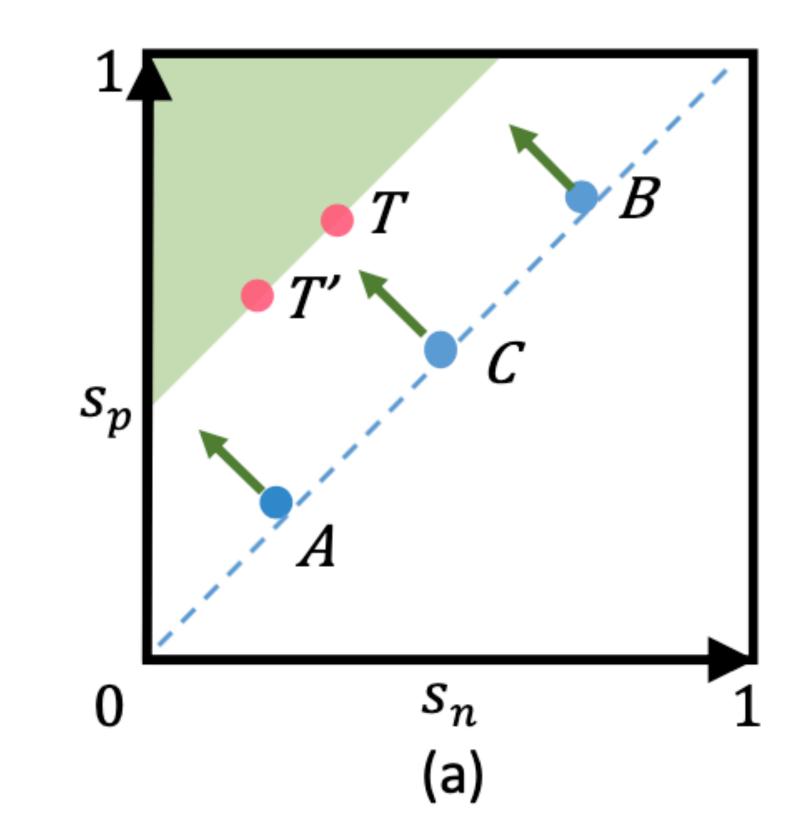
Problems:

- Lack of flexibility for optimization. The penalty strength on s_n and s_p is equal.

• Ambiguous convergence status. The decision boundary allows ambiguity for convergence.

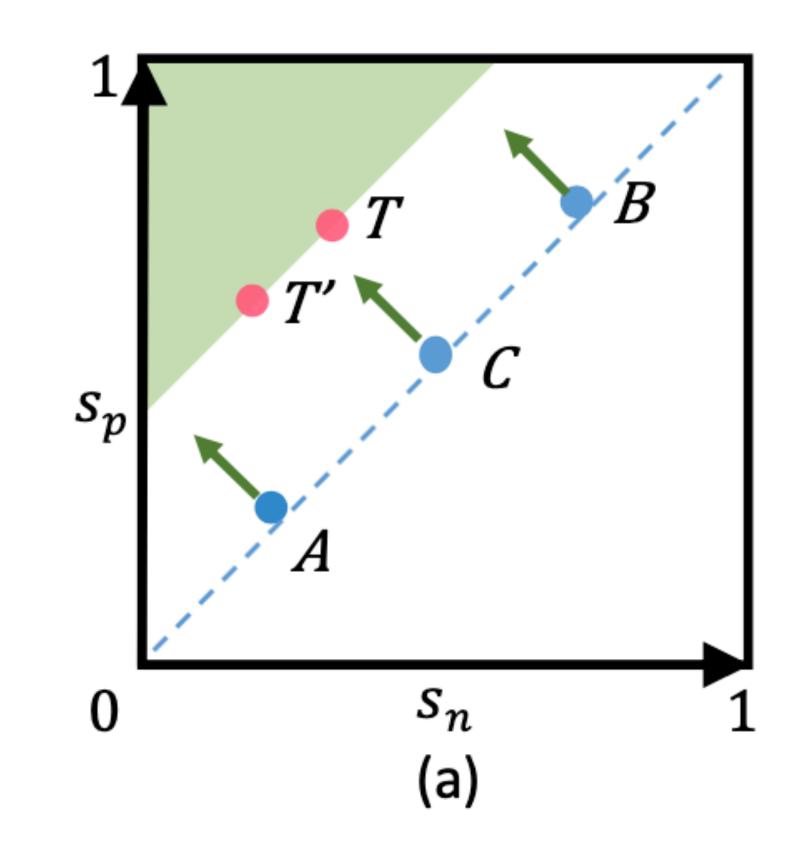


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Circle Loss

Reweight the pair:

- different similarity scores should have different penalty strength.
- the weights are linear functions w.r.t similarity scores.

 $(\alpha_n s_n)$

 $\begin{cases} \alpha_p = \\ \end{pmatrix}$ $\alpha_n =$

• if a similarity score deviates far from the optimum, it should receive strong penalty.

$$_{n} - \alpha_{p}s_{p})$$

$$\begin{split} &[O_p-s_p]_+,\\ &[s_n-O_n]_+, \end{split}$$



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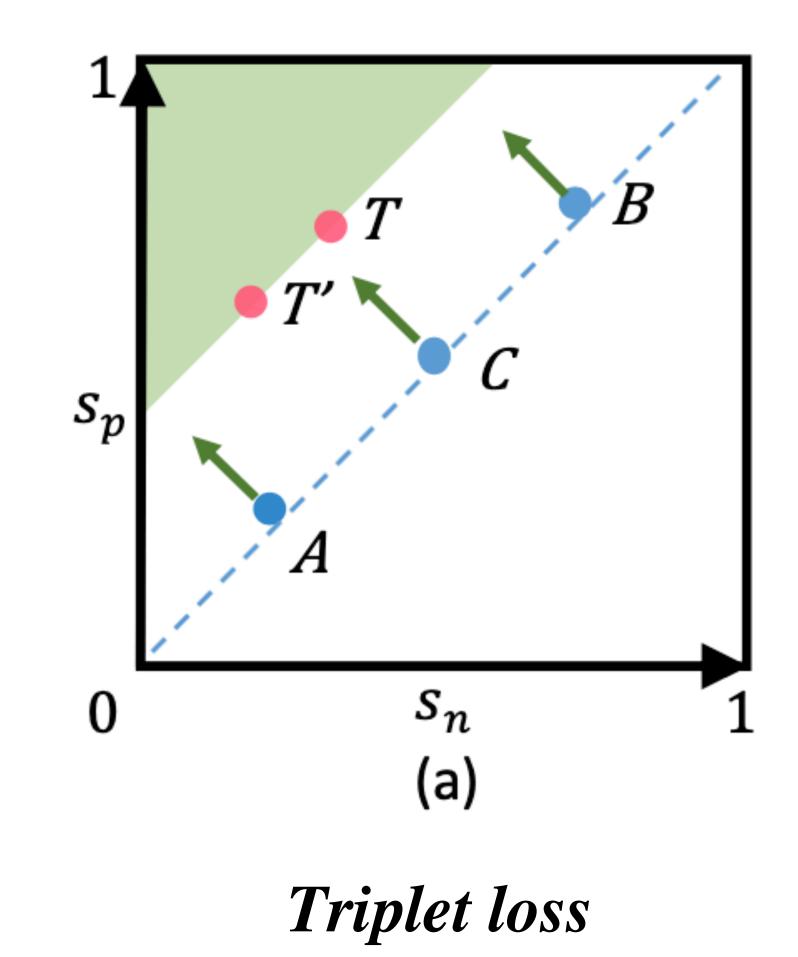
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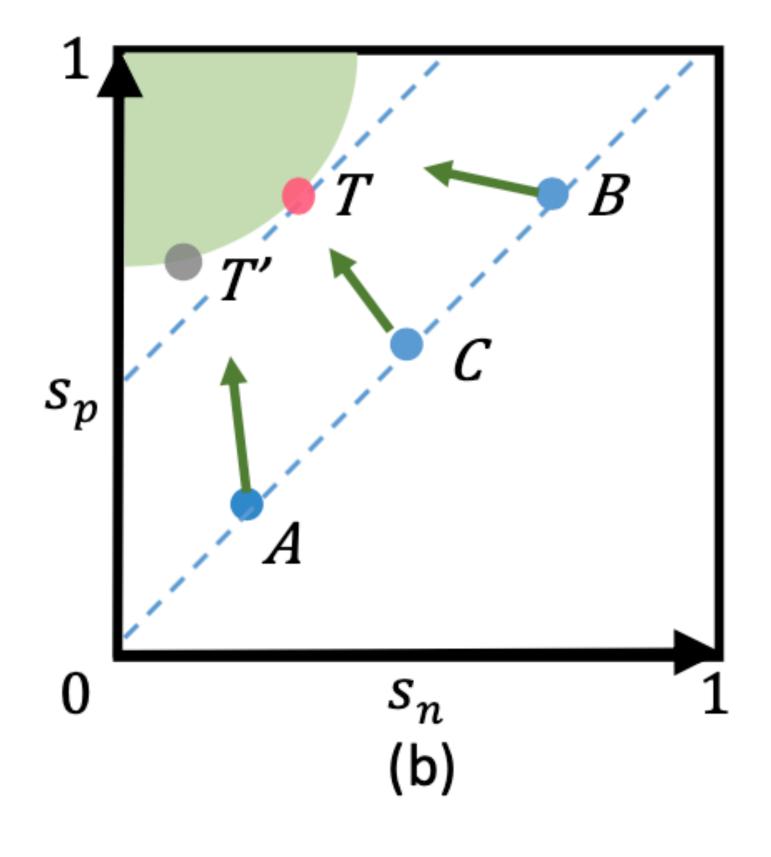
$$\left[O_{p} - \alpha_{p} s_{p} \right] + \left[O_{p} - s_{p} \right] + \left[s_{n} - O_{n} \right] + \left[s_{n} - O_{$$



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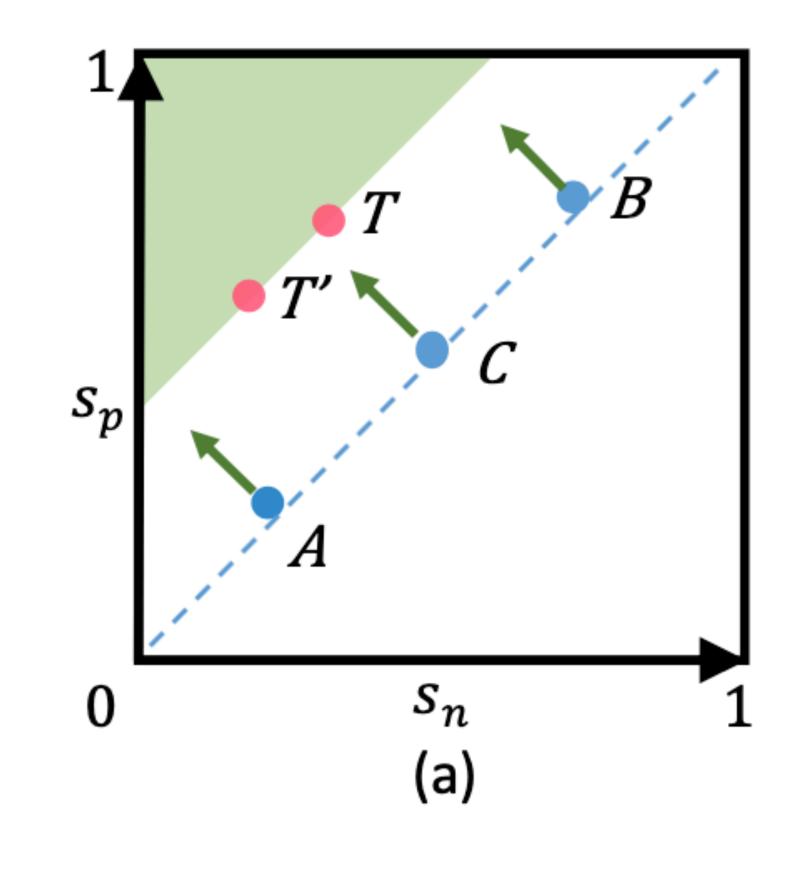
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Circle loss

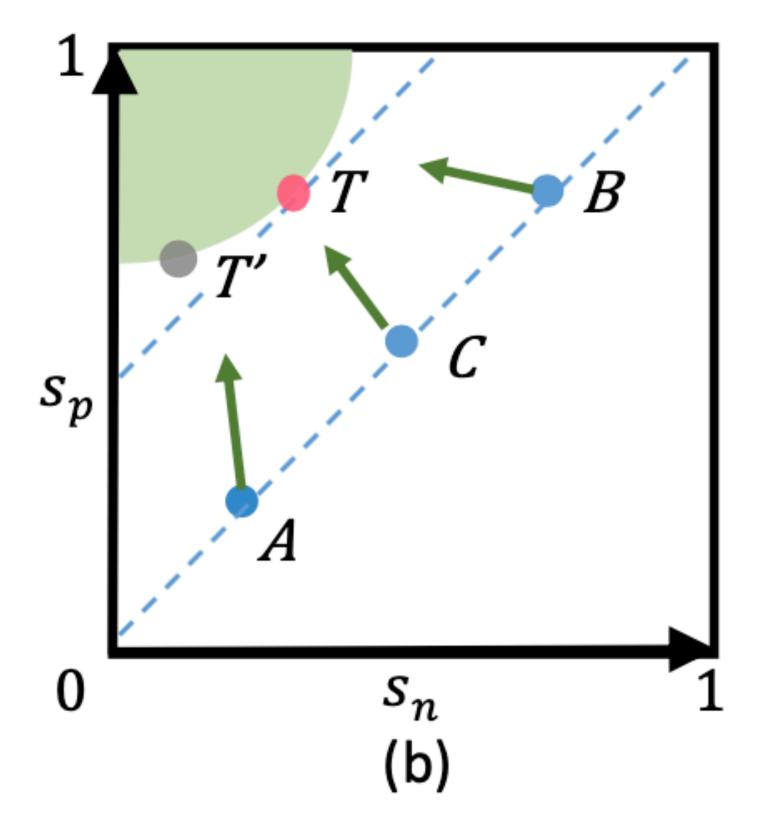


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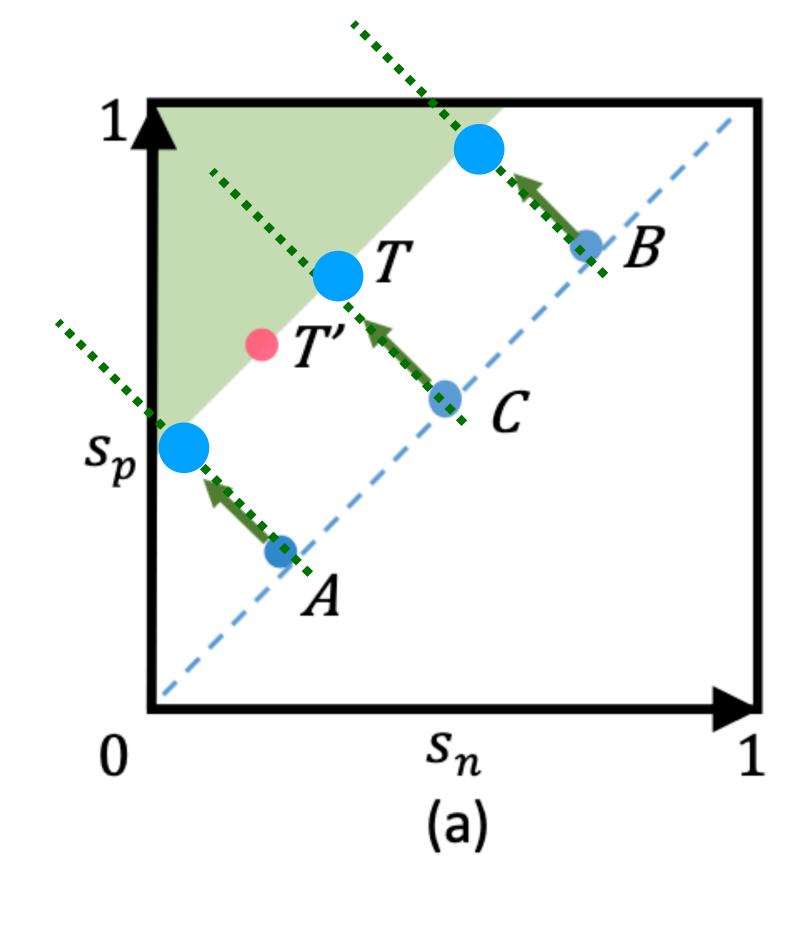
Different directions

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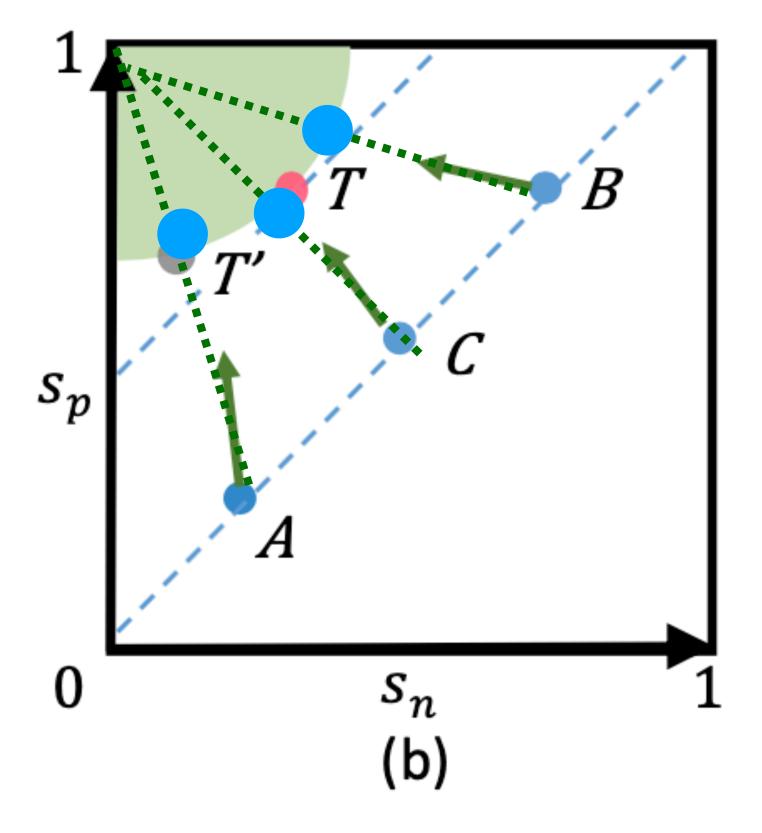




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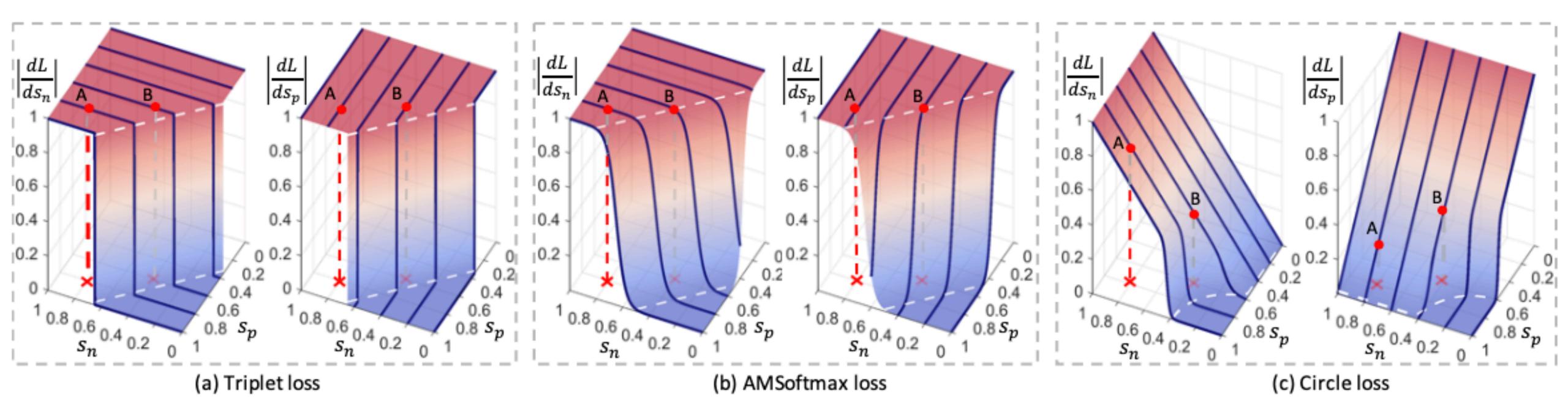
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Closer on the decision boundary



The Gradients of Losses



Circle loss assigns different gradients to the similarity scores, depending on their distances to the optimum (e.g. A and B)

Experiment: Face recognition

Table 1: Identification rank-1 accuracy (%) on MFC1 dataset with different backbones and loss functions.

Loss function	MFC1 [12] rank-1					
2000 101000	ResNet34	ResNet50	ResNet100			
Softmax	92.36	93.91	95.04			
NormFace [30]	92.62	94.12	95.27			
AM-Softmax [29, 32]	97.54	97.86	98.31			
ArcFace [2]	97.68	98.03	98.36			
CircleLoss (ours)	97.8 1	98.17	98.50			

Table 2: Face verification accuracy (%) on LFW, YTF and CFP-FP with ResNet34 backbone.

Loss function	LFW [<mark>10</mark>]	YTF [37]	CFP-FP [23]
Softmax	99.18	96.19	95.01
NormFace [30]	99.25	96.03	95.34
AM-Softmax [29, 32]	99.63	96.31	95.78
ArcFace [2]	99.68	96.34	95.84
CircleLoss(ours)	99.73	96.38	96.02

Experiment: Person re-ID

Table 4: Evaluation of Circle loss on re-ID task. We report R-1 accuracy (%) and mAP (%).

Method

PCB [26] (Softmax) MGN [31] (Softmax+Triplet) JDGL [42] ResNet50 + AMSoftmax ResNet50 + CircleLoss(ours) MGN + AMSoftmax MGN + CircleLoss(ours)

	Marke	et-1501	MSMT17			
	R-1	mAP	R-1	mAP		
	93.8	81.6	68.2	40.4		
t)	95.7	86.9	-	-		
	94.8	86.0	77.2	52.3		
	92.4	83.8	75.6	49.3		
3)	94.2	84.9	76.3	50.2		
	95.3	86.6	76.5	51.8		
	96.1	87.4	76.9	52.1		

Experiment: Fine-grained image retrieval

Loss function	CUB-200-2011 [28]			Cars196 [14]			Sta	Stanford Online Products [19]				
	R@1	R@2	R@4	R@8	R@1	R@2	R@4	R@8	R@1	R@10	$R@10^{2}$	$R@10^{3}$
LiftedStruct [19]	43.6	56.6	68.6	79.6	53.0	65.7	76.0	84.3	62.5	80.8	91.9	97.4
HDC [18]	53.6	65.7	77.0	85.6	73.7	83.2	89.5	93.8	69.5	84.4	92.8	97.7
HTL [3]	57.1	68.8	78.7	86.5	81.4	88.0	92.7	95.7	74.8	88.3	94.8	98.4
ABIER [20]	57.5	71.5	79.8	87.4	82.0	89.0	93.2	96.1	74.2	86.9	94.0	97.8
ABE [13]	60.6	71.5	79.8	87.4	85.2	90.5	94.0	96.1	76.3	88.4	94.8	98.2
Multi-Simi [34]	65.7	77.0	86.3	91.2	84.1	90.4	94.0	96.5	78.2	90.5	96.0	98.7
CircleLoss(ours)	66.7	77.4	86.2	91.2	83.4	89.8	94.1	96.5	78.3	90.5	96.1	98.6

Table 5: Comparison with state of the art on CUB-200-2011, Cars196 and Stanford Online Products. R@K(%) is reported.





Conclusion

- High flexibility in optimization.
- A more definite convergence target.

Comment

- Simple but effective
- Easy to implement
- Good presentastion of motivation

• Circle loss allows the similarity scores to learn at different paces.